

CS11-711 Advanced NLP

Pretraining

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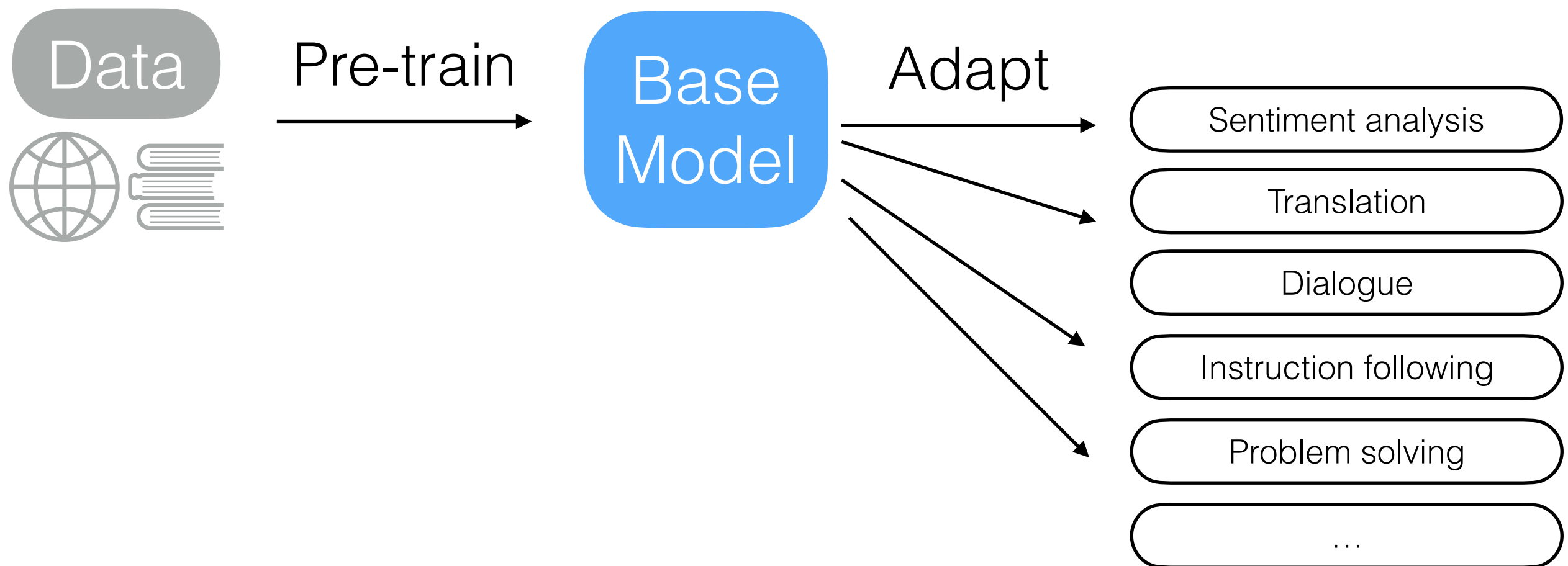


<https://cmu-l3.github.io/anlp-fall2025/>
<https://github.com/cmu-l3/anlp-fall2025-code>

Recap

- Classification, language modeling, sequence architectures
- So far:
 - Train from scratch
 - 1 model, 1 task
- Today:
 - *Pretrain a single model, adapt it to many tasks*

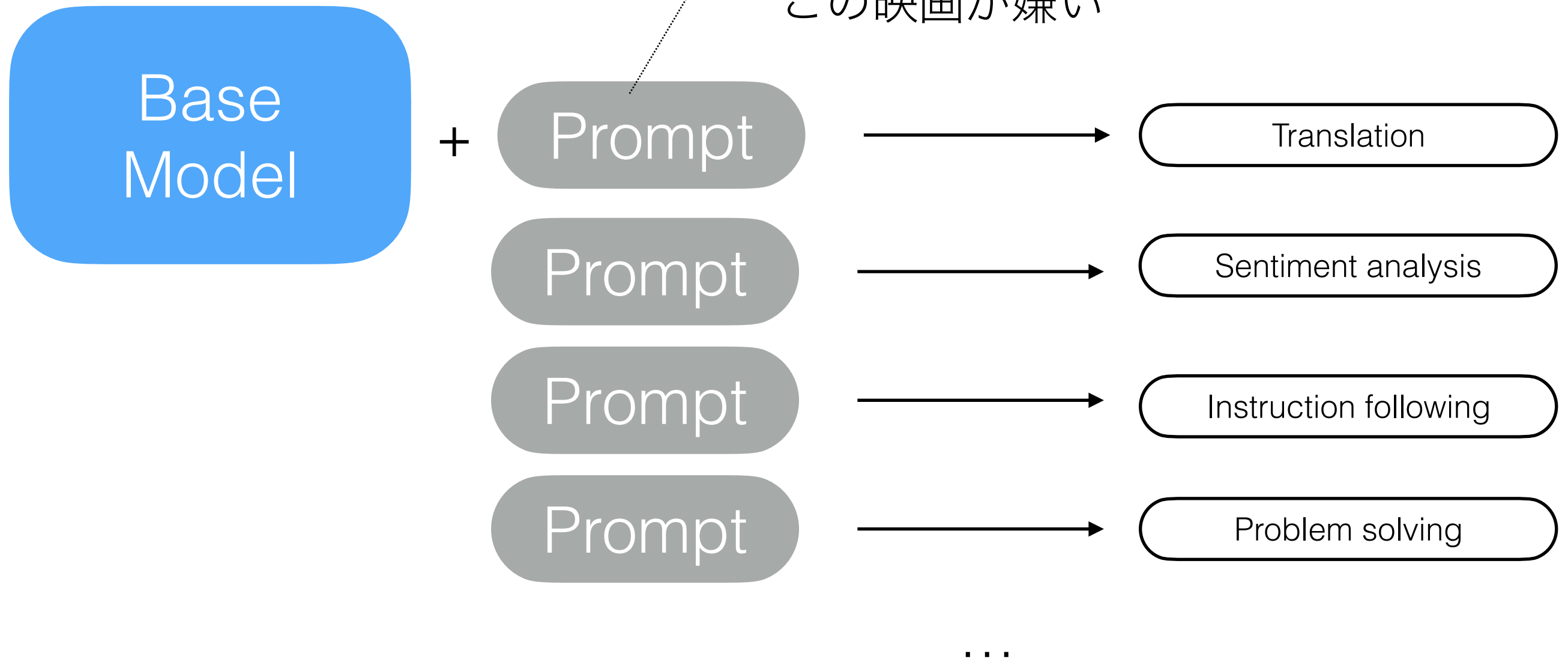
Basic idea



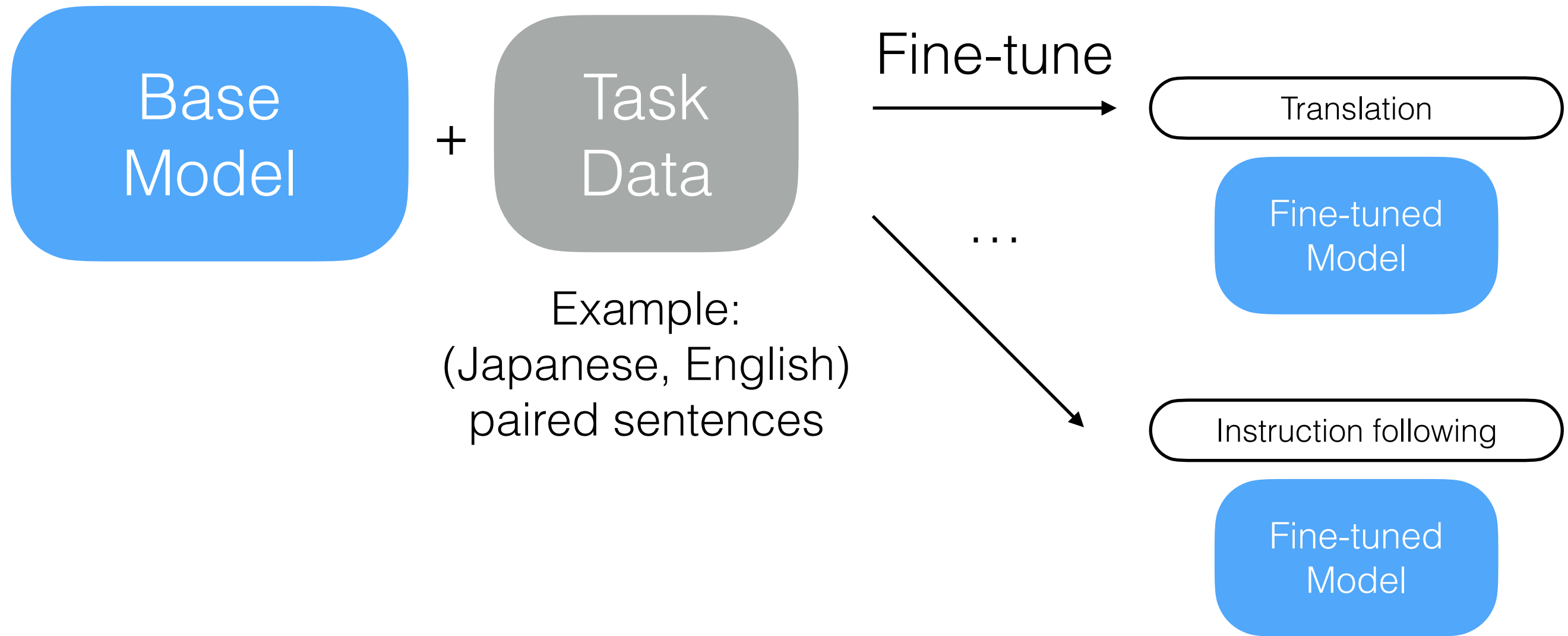
Adaptation: prompting [Lecture 7]

Example:

“Translate this sentence into English:
この映画が嫌い”



Adaptation: fine-tune [Lecture 8]



Why pre-train?

- Transfer learning: take “knowledge” from one task and apply it to another task
- **Less task data:** use less data to reach a given level of performance
- **Better task performance:** reach higher performance than training from scratch
- **One model, multiple tasks:** convenient, amortizes cost, a starting point for many uses, ...

Major factors

- Pre-trained models have names like BERT, GPT-3, Llama, Deepseek-v3, ...
- Each model is influenced by 4 major factors:
 - **Architecture:** neural network architecture
 - **Task:** what the model predicts (e.g. next-token)
 - **Data:** the data used to train the model
 - **Hyper-parameters:** e.g. learning rate, batch size

Today's lecture

- Tasks
 - Masked language modeling objective
 - Autoregressive language modeling objective
- Data: sources, quality, and quantity
- Thinking about pretraining
 - Tokens, model size, compute
 - Scaling laws

Masked Language Modeling

- Predict masked tokens x_M given visible tokens $x_{\neg M}$



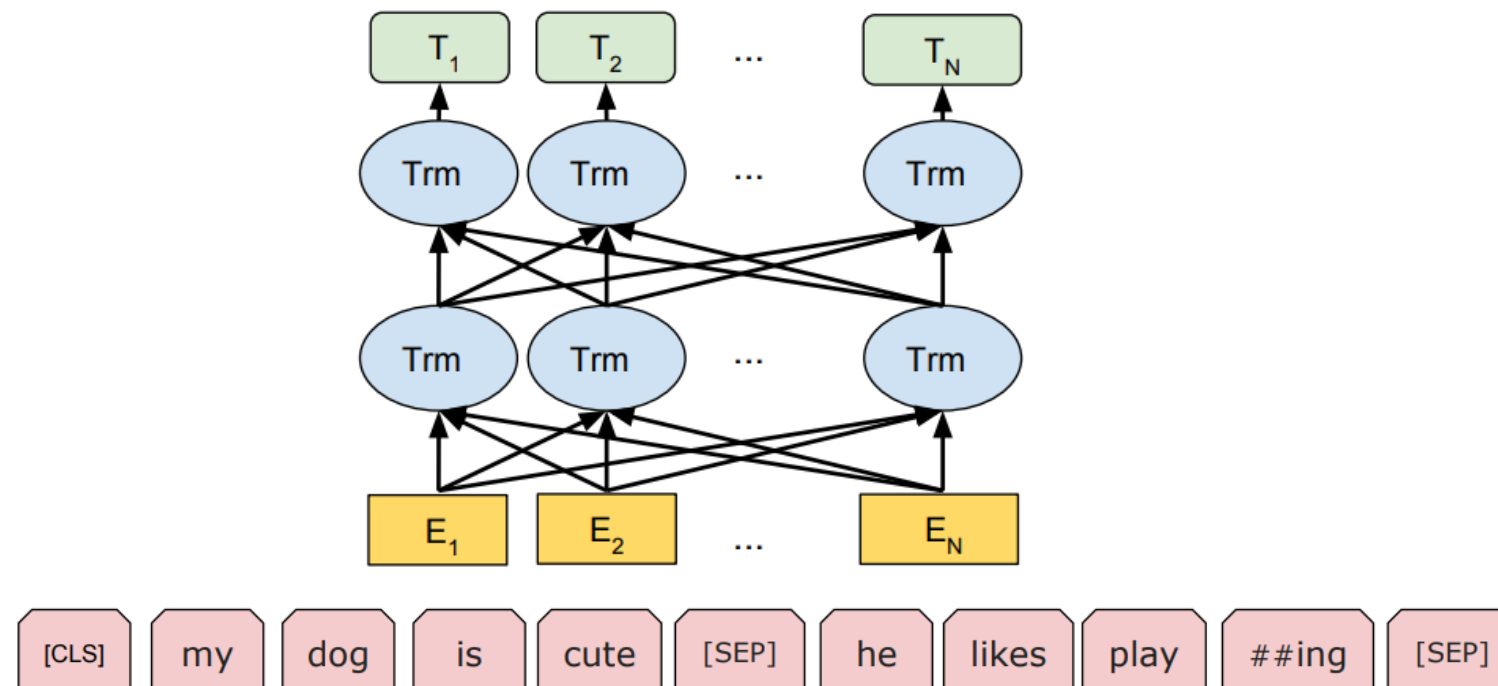
$$\mathcal{L}_{\text{MLM}}(\theta; D) = -\frac{1}{|D|} \sum_{x \in D} \mathbb{E}_{M \sim \text{corrupt}(x)} \sum_{t \in M} \log p_{\theta}(x_t | x_{\neg M})$$

- View as *denoising*: corrupt $x \rightarrow$ reconstruct x
- Maximizes *pseudo-likelihood*

Example: BERT

(Devlin et al. 2018)

- **Model:** Transformer



- **Data:** BooksCorpus + English Wikipedia
- **Task:** Masked language modeling

Example: BERT

(Devlin et al. 2018)

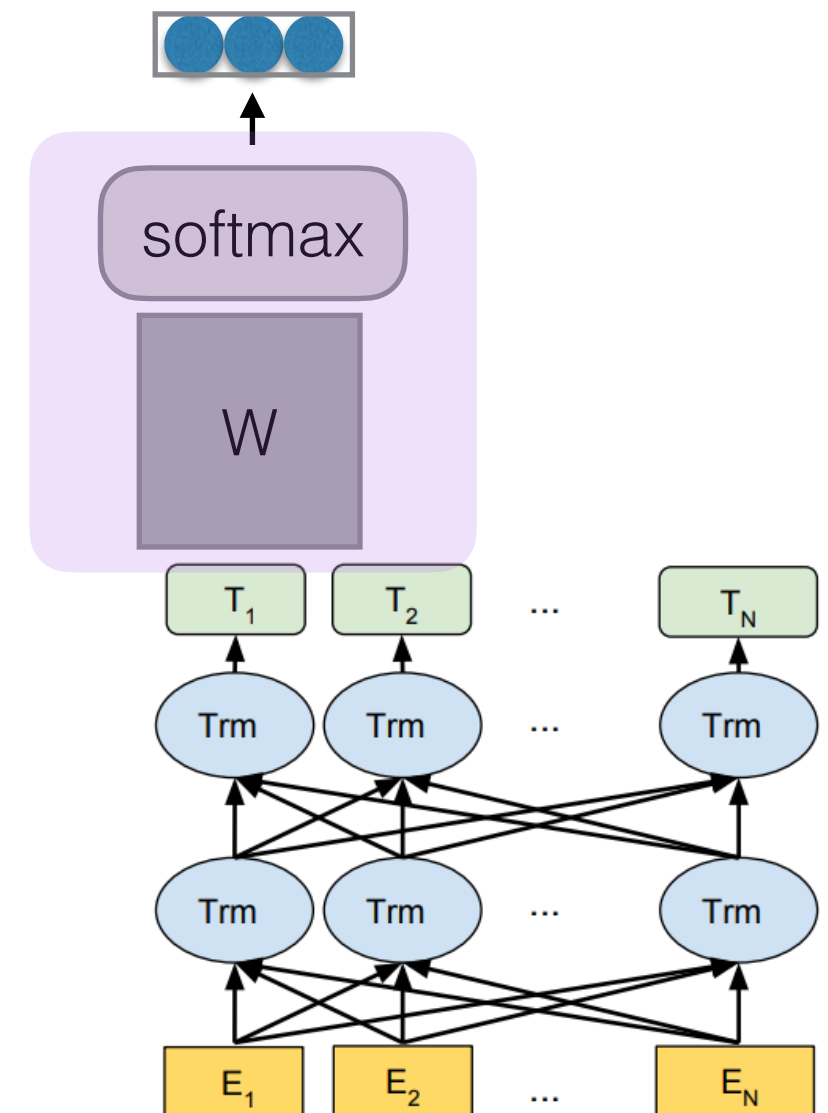
Predict a masked token

- 80%: substitute input token with [MASK]
- 10%: substitute input token with random token
- 10%: no change



Adapting a masked language model

- Add an output layer that maps a hidden vector to scores
- Fine-tune the weights (either just W , or all weights). Example:
 - Data: (movie review, {positive, neutral, negative})
 - Initialize the model with BERT
 - Minimize cross-entropy loss with gradient-based optimization

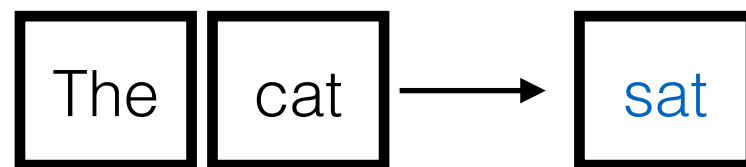


Today's lecture

- Tasks
 - Masked language modeling
 - **Autoregressive language modeling**

Autoregressive language modeling

- Predict next token x_t given previous tokens $x_{<t}$



$$\mathcal{L}_{\text{MLE}}(\theta; D) = -\frac{1}{|D|} \sum_{x \in D} \sum_{t=1}^{|x|} \log p_{\theta}(x_t | x_{<t})$$

- Maximizes likelihood
 - Fits a data distribution p_*
 - Learns to *compress* data generated by p_*

Maximum likelihood: fits a data distribution

- Makes p_θ match the data distribution p_{data} (p_* for brevity)

$$\begin{aligned}\min_{\theta} D_{KL}(p_* || p_\theta) &= \min_{\theta} - \sum_{x \in \mathcal{X}} p_*(x) \log \frac{p_\theta(x)}{p_*(x)} \\ &\equiv \min_{\theta} - \sum_{x \in \mathcal{X}} p_*(x) \log p_\theta(x) + \text{const} \\ &= \min_{\theta} - \mathbb{E}_{x \sim p_*} \log p_\theta(x)\end{aligned}$$

Dataset:
samples from p_*

$$\approx \min_{\theta} - \frac{1}{|D|} \sum_{x \in D} \log p_\theta(x)$$

$$\equiv \max_{\theta} \sum_{x \in D} \log p_\theta(x)$$

Maximum
likelihood!

Maximum likelihood: learns to compress

- Goal: compress data from a distribution p_* into a binary code, $c(x_{1:n}) \rightarrow \{0,1\}^*$
- *Arithmetic coding* turns a distribution p into a code $c(\cdot)$
- Minimum expected code length is the entropy [Shannon 1948]:

$$H(p_*) = \mathbb{E}_{x \sim p_*} \left[- \sum_{i=1}^N \log_2 p_*(x_i | x_{<i}) \right]$$

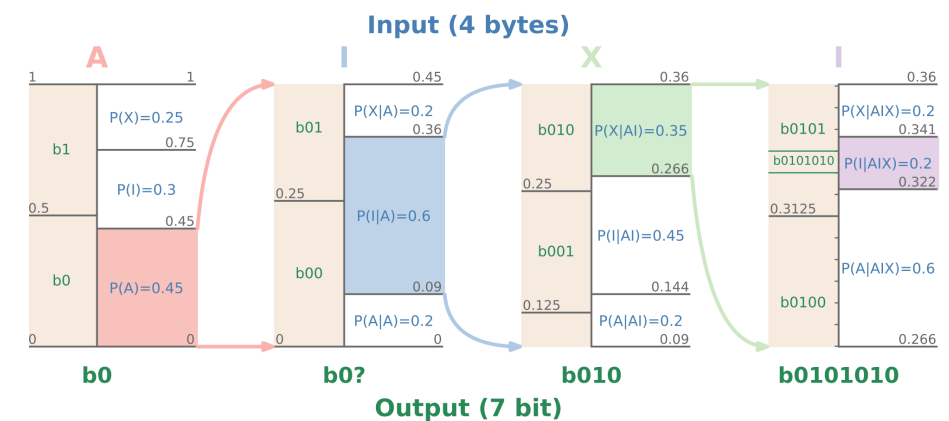


Figure: [Deletang et al 2024]

- When we use a model p_θ , the expected code length is the cross-entropy:

$$H(p_*, p_\theta) = \mathbb{E}_{x \sim p} \left[- \sum_{i=1}^N \log_2 p_\theta(x_i | x_{<i}) \right]$$

$$H(p_*, p_\theta) = H(p_*) + KL(p_* \| p_\theta)$$

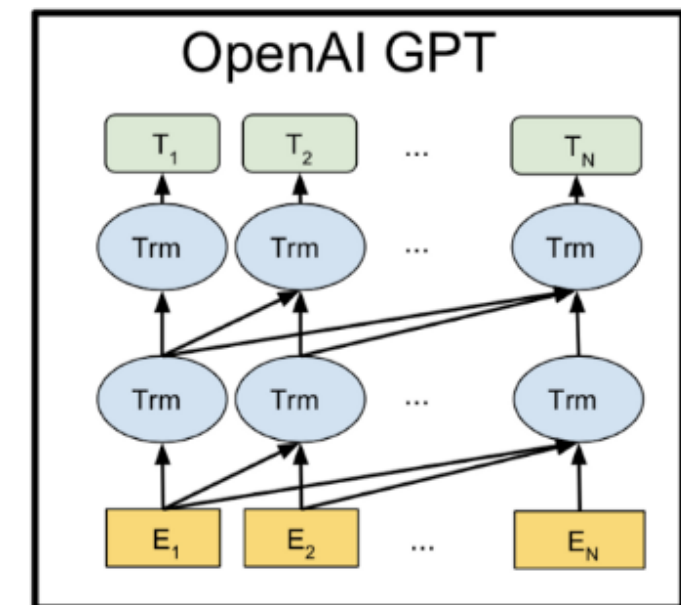
To achieve the minimum expected code length $H(p_*)$, minimize KL divergence via MLE

Key factors

$$\mathcal{L}_{\text{MLE}}(\theta; D) = - \mathbb{E}_{x \sim D} \sum_{t=1}^{|x|} \log p_{\theta}(x_t | x_{<t})$$

- Things we can change:
 - θ : model architecture and size
 - D : training data
 - Optimization hyper-parameters, e.g. learning rate, batch size

Example: GPT-2



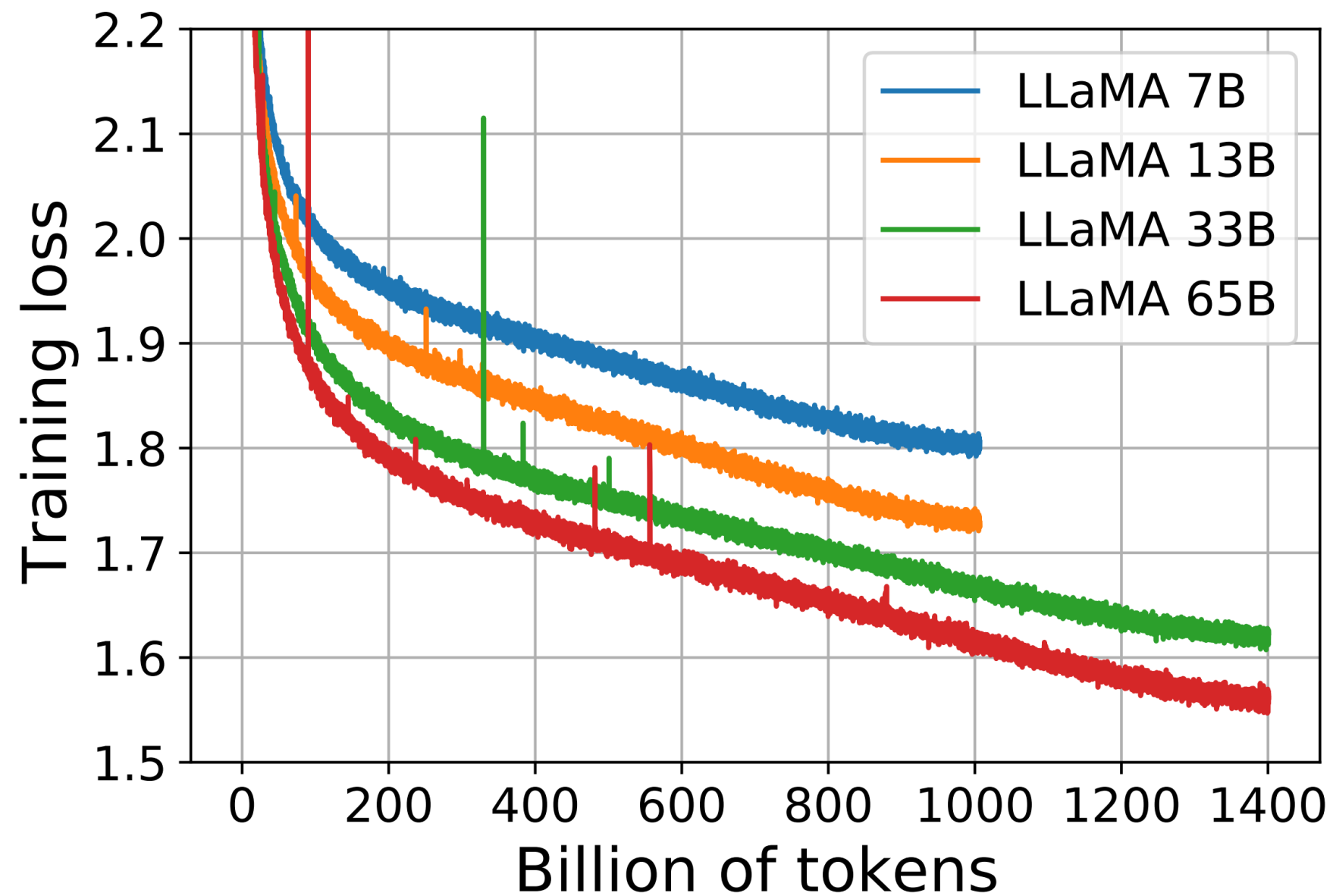
- **Model:** Transformer (1.5B)
- **Data:** WebText (millions of web pages)

Example: Llama

- **Model:** Transformer, {6.7B, 13B, 32B, 65B}
- **Data:** 1.4 trillion tokens, sources:

Dataset	Sampling prop.	Epochs	Disk size
CommonCrawl	67.0%	1.10	3.3 TB
C4	15.0%	1.06	783 GB
Github	4.5%	0.64	328 GB
Wikipedia	4.5%	2.45	83 GB
Books	4.5%	2.23	85 GB
ArXiv	2.5%	1.06	92 GB
StackExchange	2.0%	1.03	78 GB

Llama: training loss

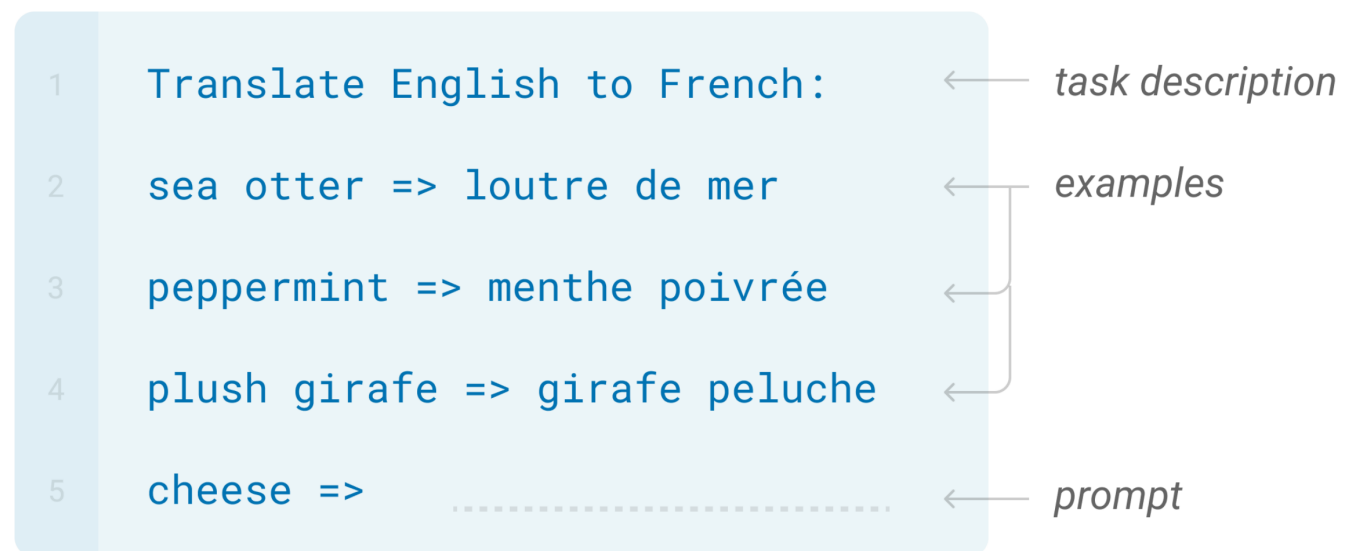


Evaluating a model

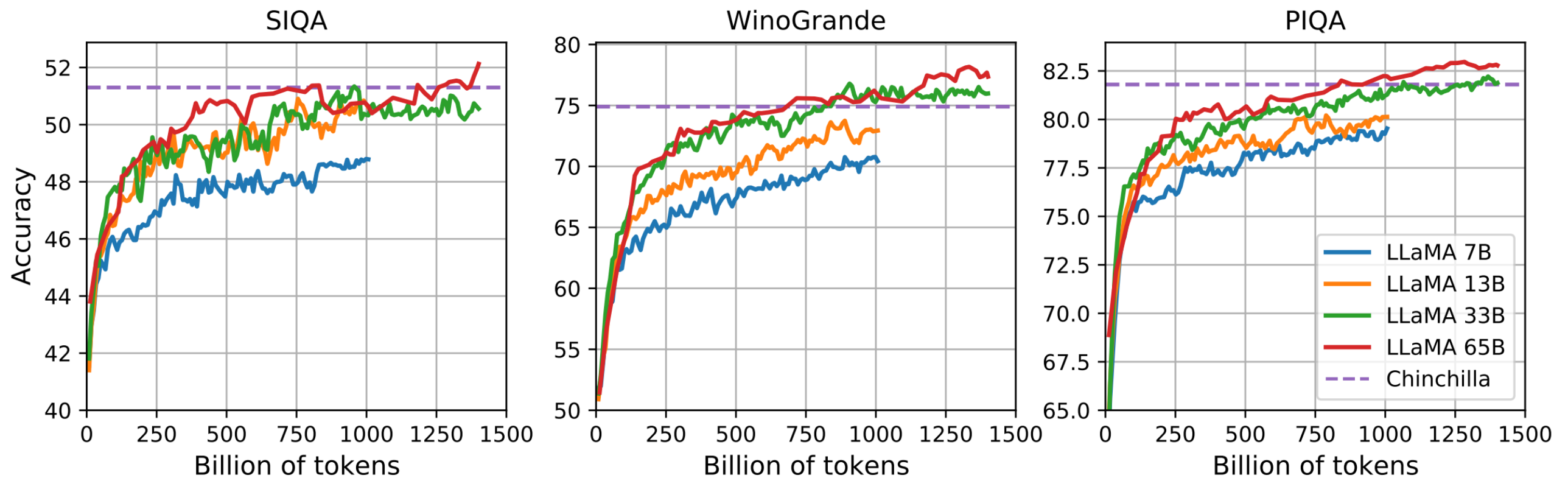
- Loss (training, validation, test)
- Diagnose training trajectory, compare models in the same family

- Few-shot prompting

- Fine-tuning



Llama: few-shot performance trajectory



Practical tools: HuggingFace

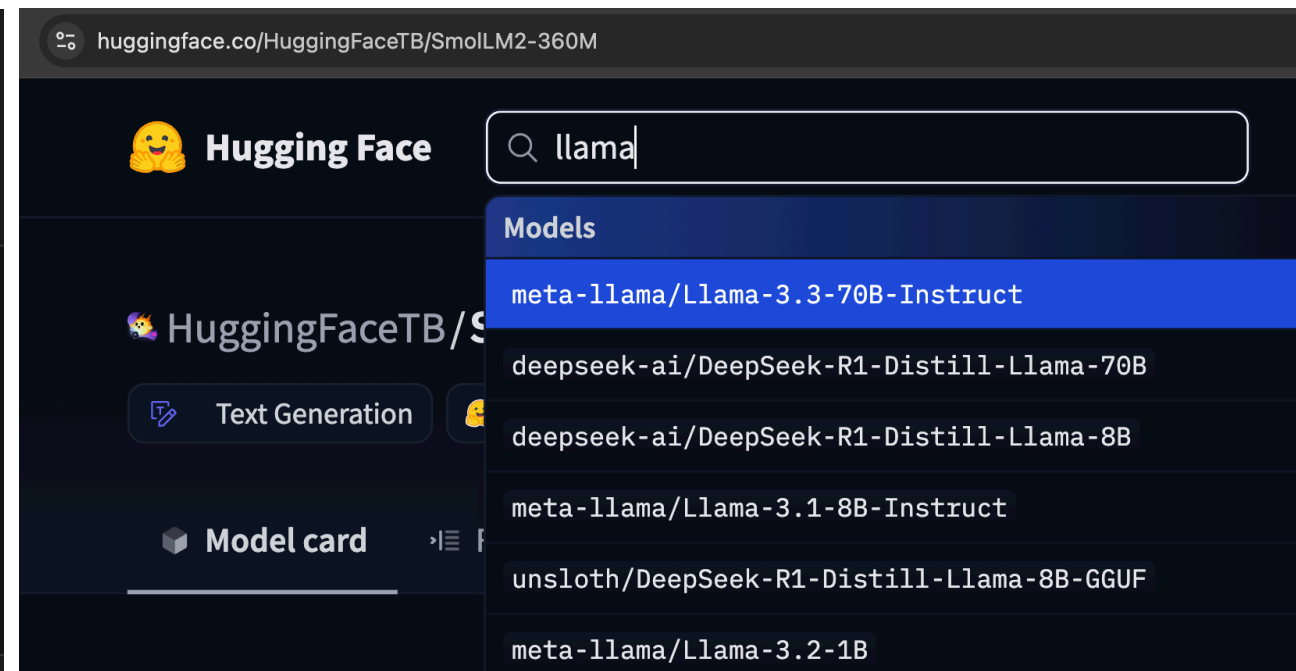
Load tokenizer and model

- Find models at <https://huggingface.co/>

```
from transformers import AutoTokenizer, AutoModelForCausalLM

model = "HuggingFaceTB/SmolLM2-360M"

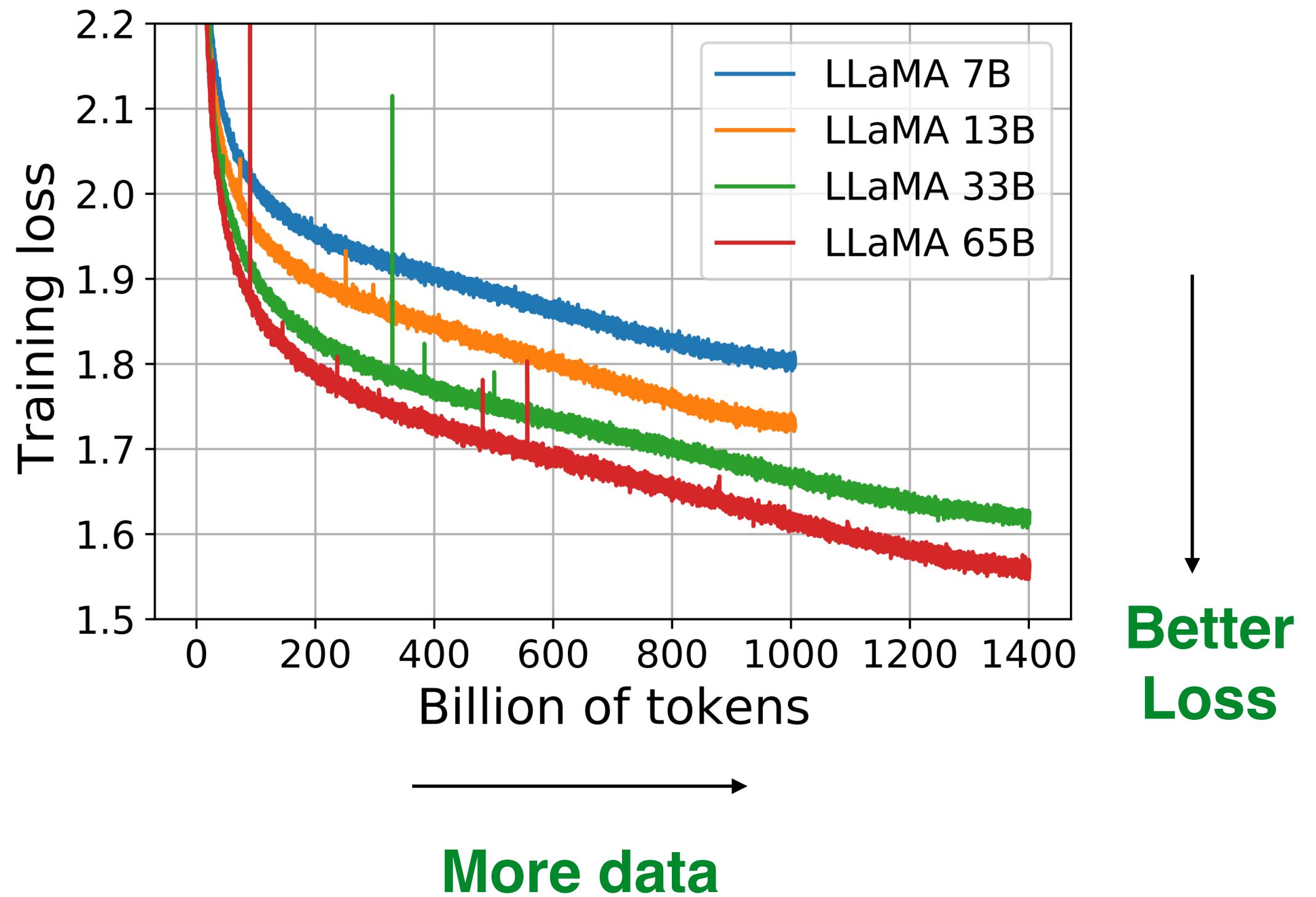
tokenizer = AutoTokenizer.from_pretrained(model)
model = AutoModelForCausalLM.from_pretrained(model)
```



https://github.com/cmu-l3/anlp-fall2025-code/blob/main/06_pretraining/pretraining.ipynb

Today's lecture

- Tasks
- **Data:** sources, quality, and quantity



Data factors

- **Quantity**: How much data do I have?
- **Quality**: Is it beneficial for training?
- **Coverage**: Does the data cover the domain(s) I care about, and in the right proportions?

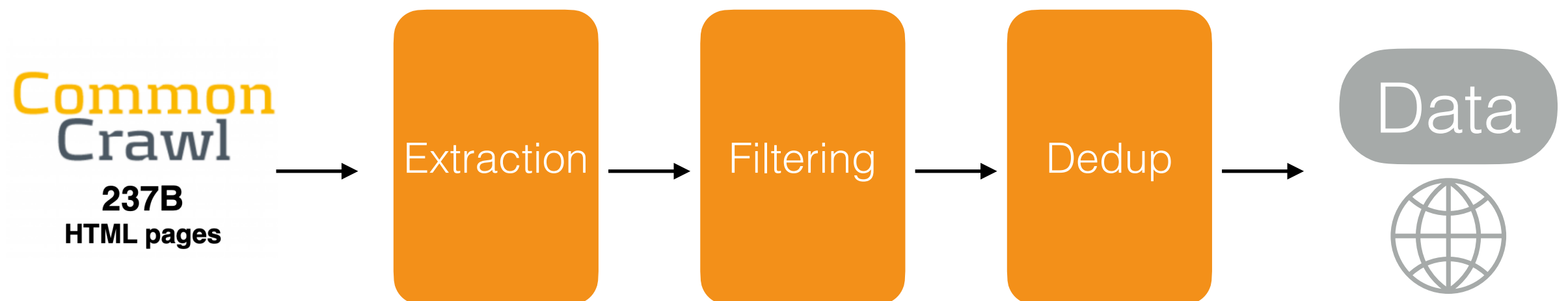
Data quantities

	Tokens of training data
Llama 1	1.4 trillion
Llama 2	1.8 trillion
Llama 3	15 trillion
Deepseek 3	15 trillion

Wikipedia: < 10 billion

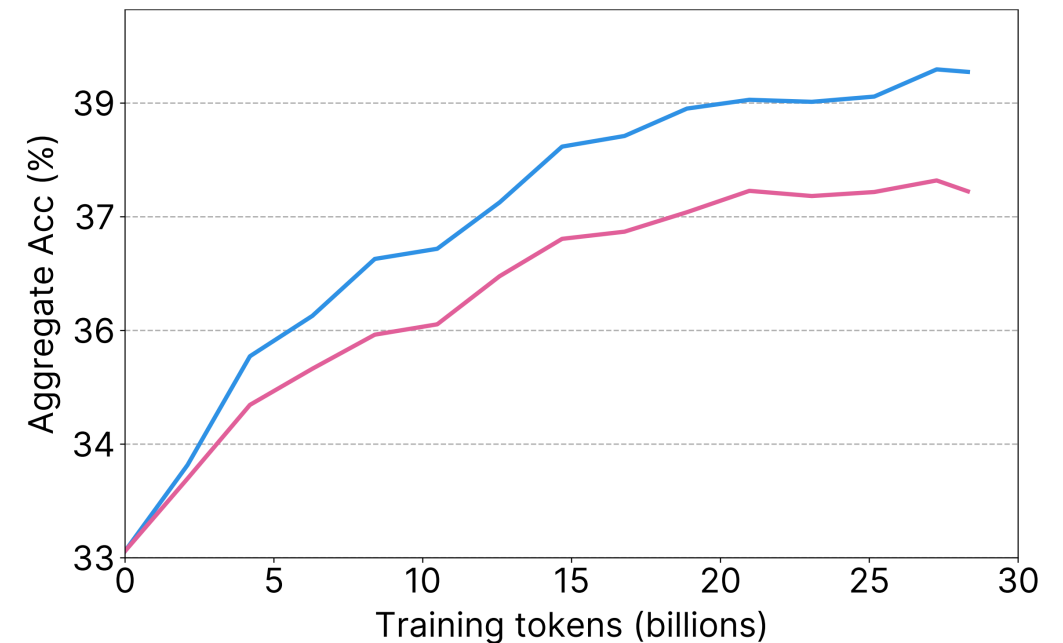
Web data: common crawl

- Large snapshots of web pages.
 - Extraction: HTML to text
 - Filtering: filter out unwanted pages
 - Deduplication: many duplicate web pages



Quality: Extraction

- Extraction: HTML to text
- Remove boilerplate
- Retain Latex, code, etc.



This paper concerns the quantity
``, defined as the length of the longest subsequence of the numbers from

Image Equations

Suppose I have a smooth map
`[tex]f\colon \mathbb{R}^3 \rightarrow S^2[/tex]`. If I identify `[tex]\mathbb{R}^3` with `[tex]U_S = S^3 - \{(0,0,1)\}` via stereographic projection

Delimited Math

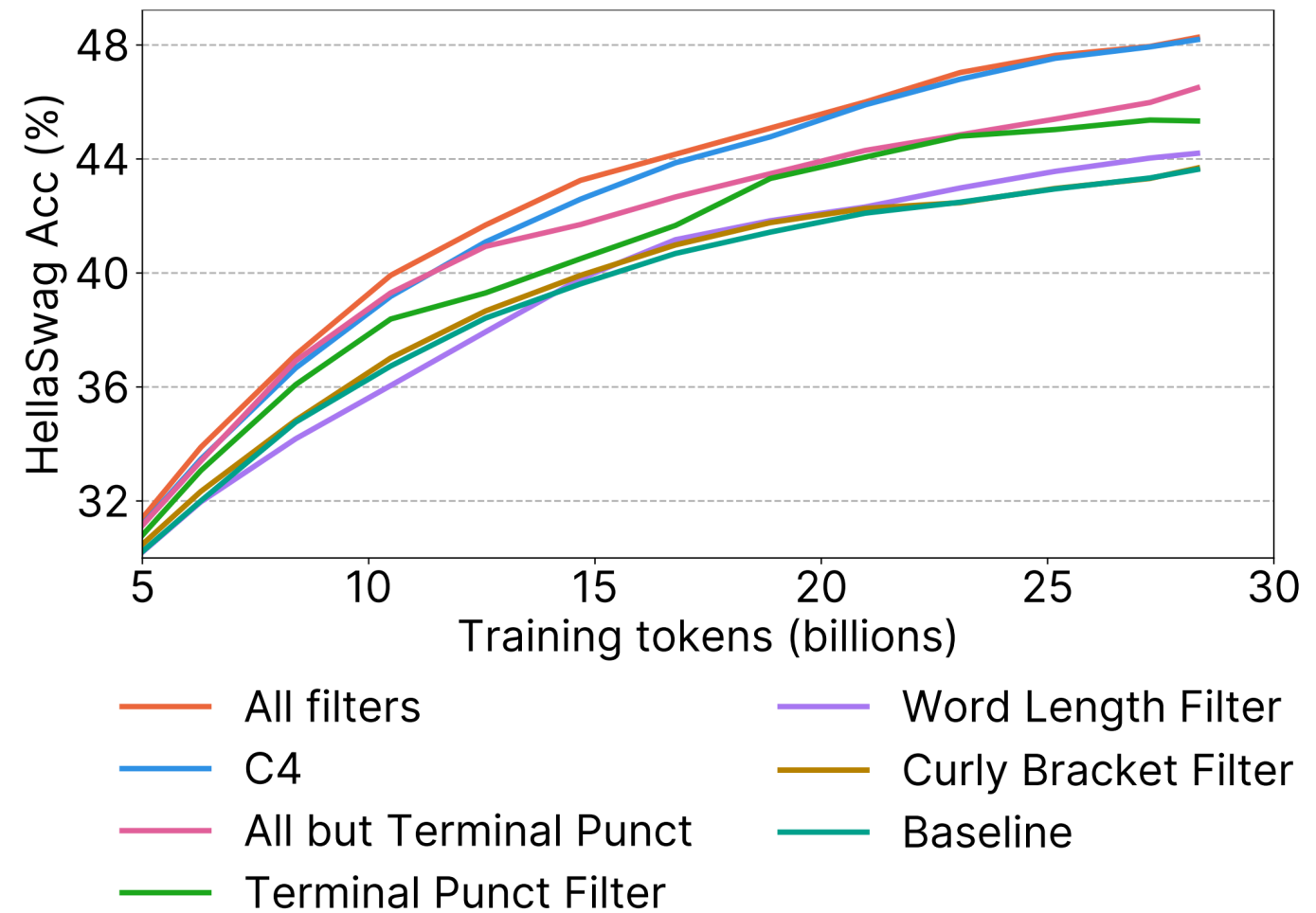
...
`Penedo et al 2024`
`{\displaystyle \mathrm {MA} ={\frac {f_{0}}{f_{E}}}}`
`</annotation>`
`</semantics>`
`</math>`

Special Tags

Paster et al 2023

Quality: Filtering

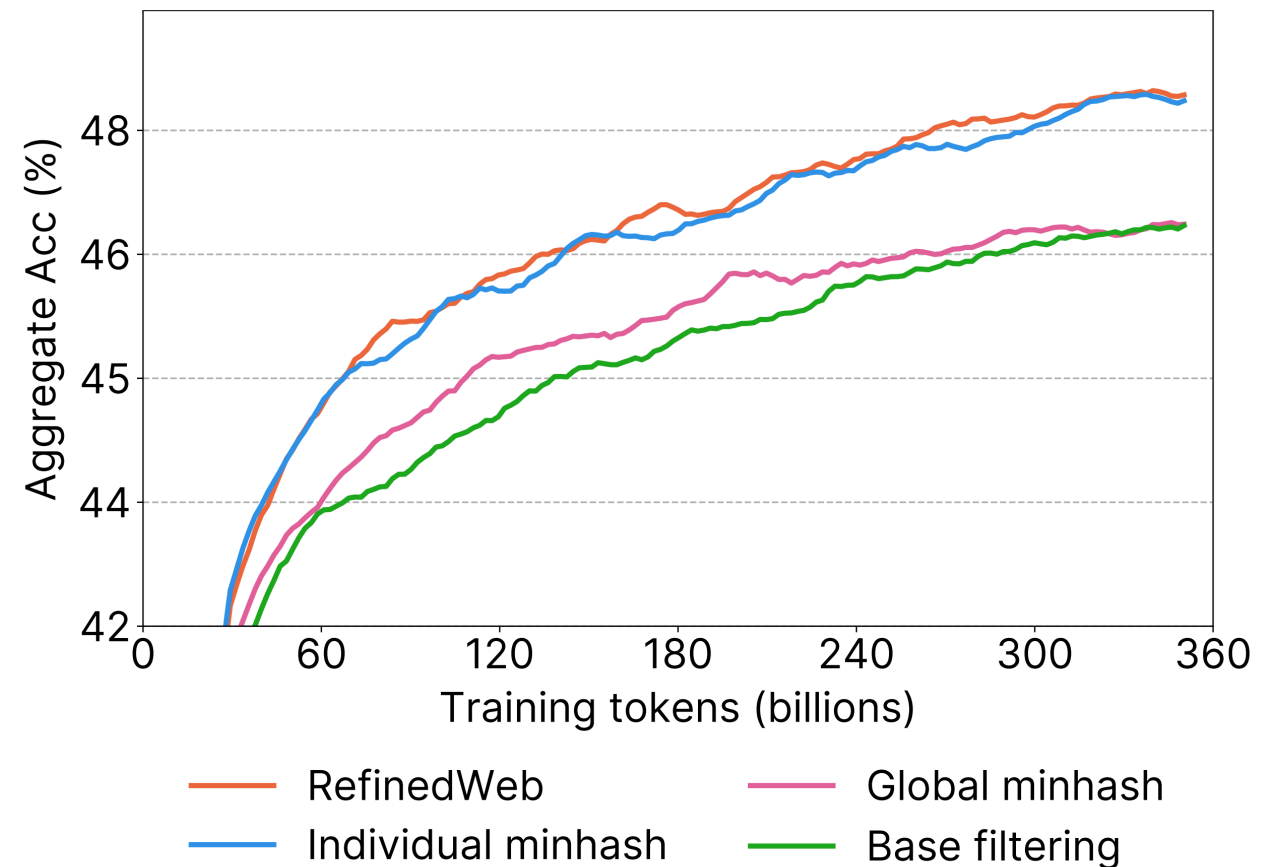
- Filter out unwanted text
- Language filter
- Repetitions
- Too many short lines
- ...



Penedo et al 2024

Quality: Deduplication

- Remove duplicate content
- Fuzzy strategy: *minhash*
- Too much deduplication can be harmful
- [Penedo et al 2024]:
Deduplicate per-snapshot
rather than globally



Penedo et al 2024

Example (Dolma)

```
added 2023-04-11T09:57:03.044571+00:00
attributes {'random_number_v1__random_number_v1__random': [[0, 9626, 0.11918]]}
created 2020-01-17T12:48:23Z
id http://250news.theexplorationplace.com/www.250news.com/65595.html
metadata {'bucket': 'head', 'cc_segment': 'crawl-data/CC-MAIN-2020-05/segments/1'}
source common-crawl
text Prince George, B.C.— Construction of the new RiverBend Seniors housing project.
The $33 million dollar project was first presented to Mayor and Council in 2013.
Hall and key members of the City Staff, arranged to meet with Quinn in Kamloops.
“This project comes at the perfect time for us” says Gwen Norheim. She and her husband
Quinn says they did make an interesting discovery when they started construction.
That’s it, big smiles Shirley and Mike... there is an election coming.
This is an excellent and well needed project!
If the NDP was in power (god forbid) and it was NDP MLA’s in the picture, you would
Go ahead and deny it if you want, but we know better!
What we do know with the liberals is they are always raising fees and medical costs
grow up galt.
```

https://github.com/cmu-l3/anlp-fall2025-code/blob/main/06_pretraining/pretraining.ipynb

Data factors

- Quantity: How much data do I have?
- Quality: Is it beneficial for training?
- **Coverage**: Does the data cover the domain(s) I care about, and in the right proportions?

Coverage

- The data determines the data distribution
 - And hence the model, $p_{\theta} \approx p_{data}$
- Web data \neq math data
- Web data \neq educational data
- Web data \neq code data
- ...

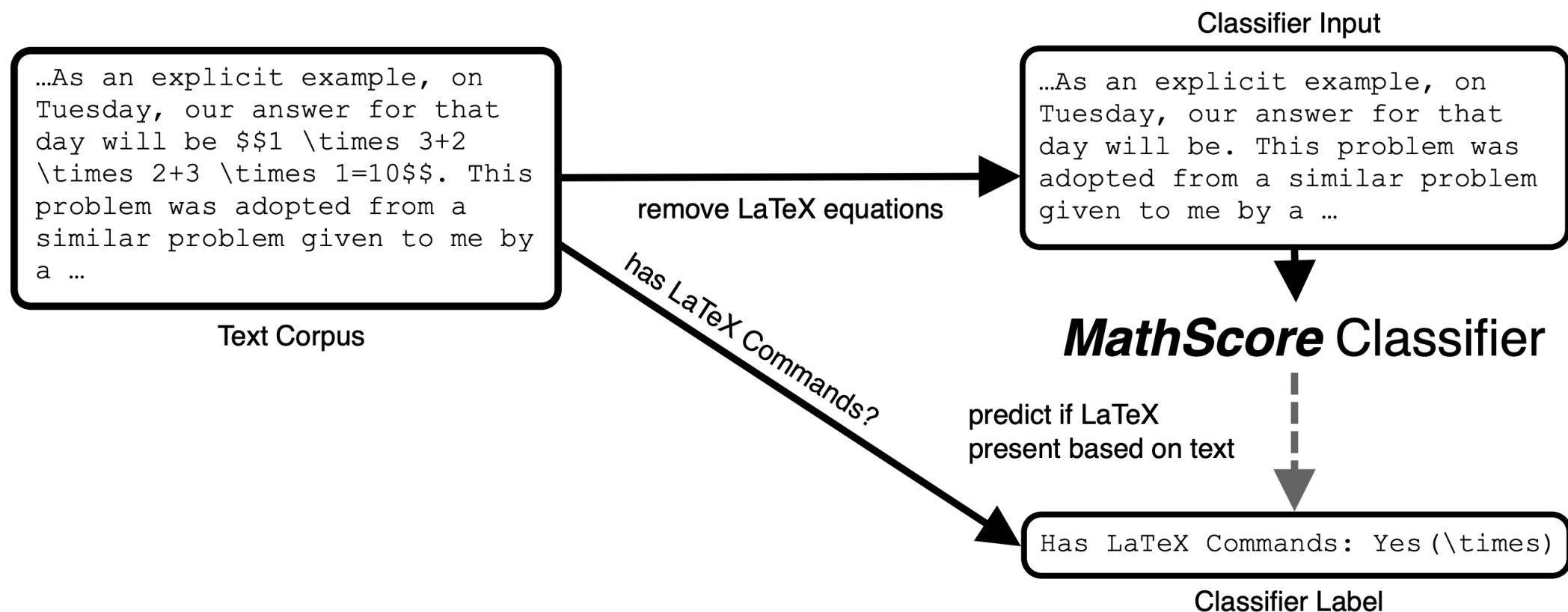
Approach: classifier filtering

- Train a classifier to detect desired data
- Use it to filter out undesired data



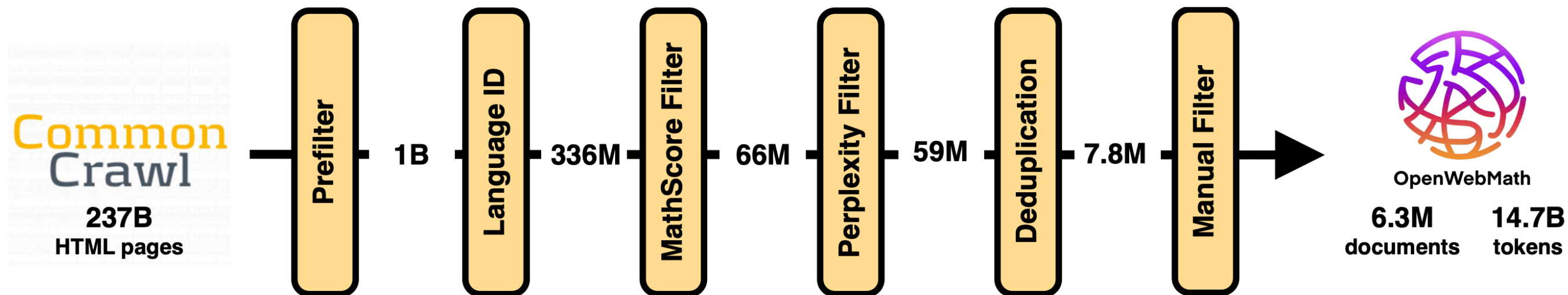
Approach: classifier filtering

- Example: **OpenWebMath** [Paster et al 2023]
 - MathScore classifier detects math content



Approach: classifier filtering

- Example: **OpenWebMath** [Paster et al 2023]
- MathScore classifier detects math content



Approach: classifier filtering

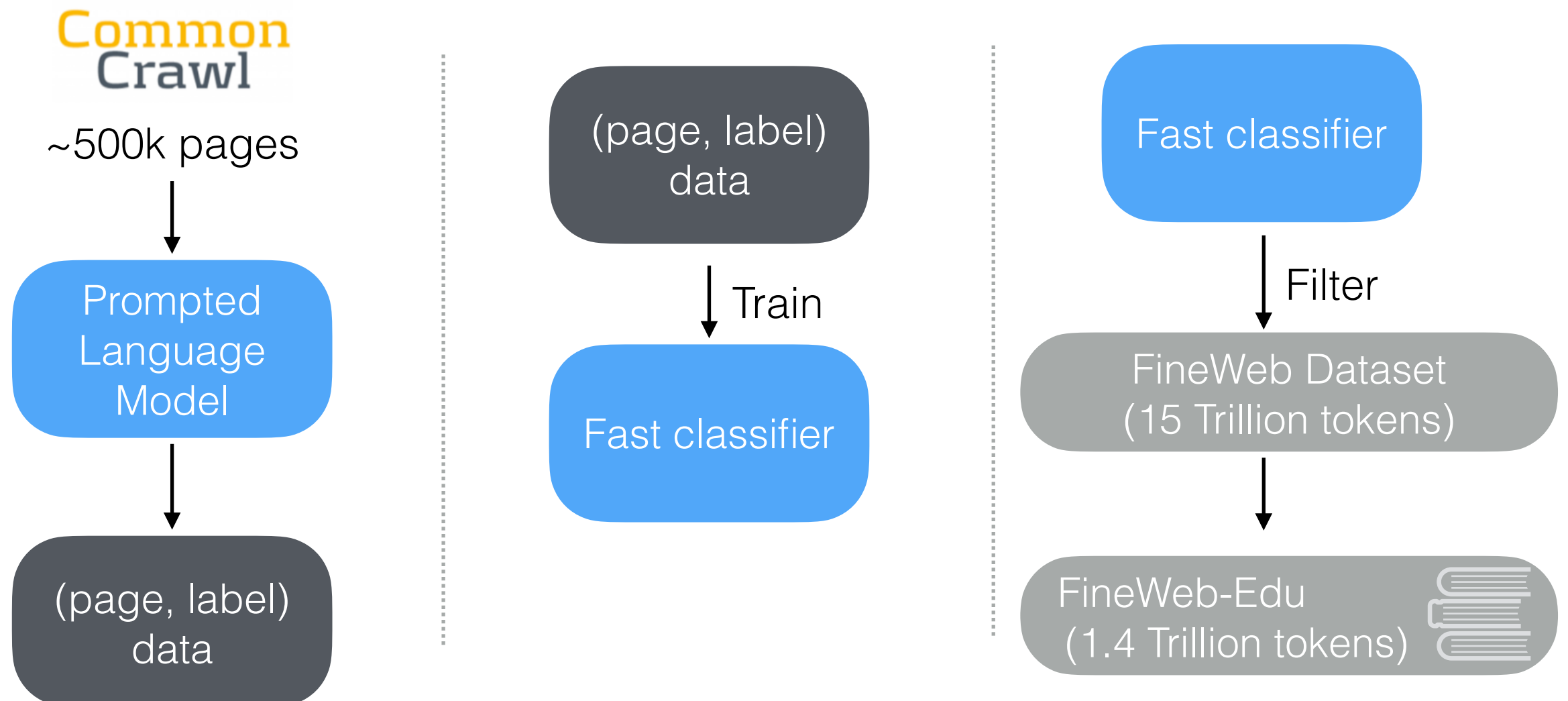
- Example: **OpenWebMath** [Paster et al 2023]

Domain	# Characters	% Characters
stackexchange.com	4,655,132,784	9.55%
nature.com	1,529,935,838	3.14%
wordpress.com	1,294,166,938	2.66%
physicsforums.com	1,160,137,919	2.38%
github.io	725,689,722	1.49%
zbmath.org	620,019,503	1.27%
wikipedia.org	618,024,754	1.27%
groundai.com	545,214,990	1.12%
blogspot.com	520,392,333	1.07%
mathoverflow.net	499,102,560	1.02%

<https://huggingface.co/datasets/open-web-math/open-web-math>

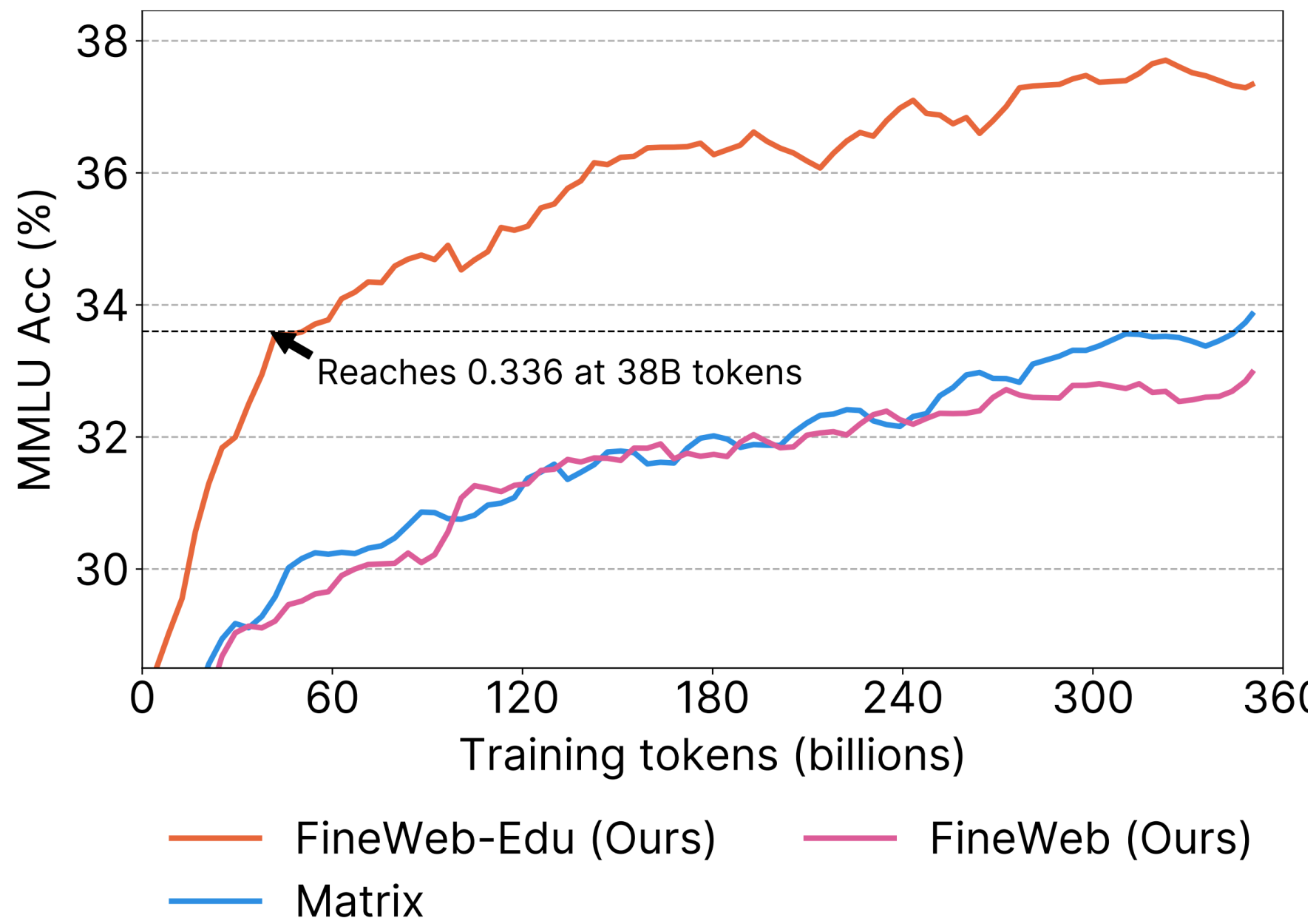
Approach: classifier filtering

- Example: **FineWeb-Edu** [Penedo et al 2024]
- Classifier to classify pages as “educational”



Approach: classifier filtering

- Example: **FineWeb-Edu** [Penedo et al 2024]



Mixtures

- In practice, training data is a mixture of different sources

Source	Type	Tokens
Pretraining ♦ OLMo 2 1124 Mix		
DCLM-Baseline	Web pages	3.71T
StarCoder filtered version from OLMoE Mix	Code	83.0B
peS2o from Dolma 1.7	Academic papers	58.6B
arXiv	STEM papers	20.8B
OpenWebMath	Math web pages	12.2B
Algebraic Stack	Math proofs code	11.8B
Wikipedia & Wikibooks from Dolma 1.7	Encyclopedic	3.7B
Total		3.90T

Recap

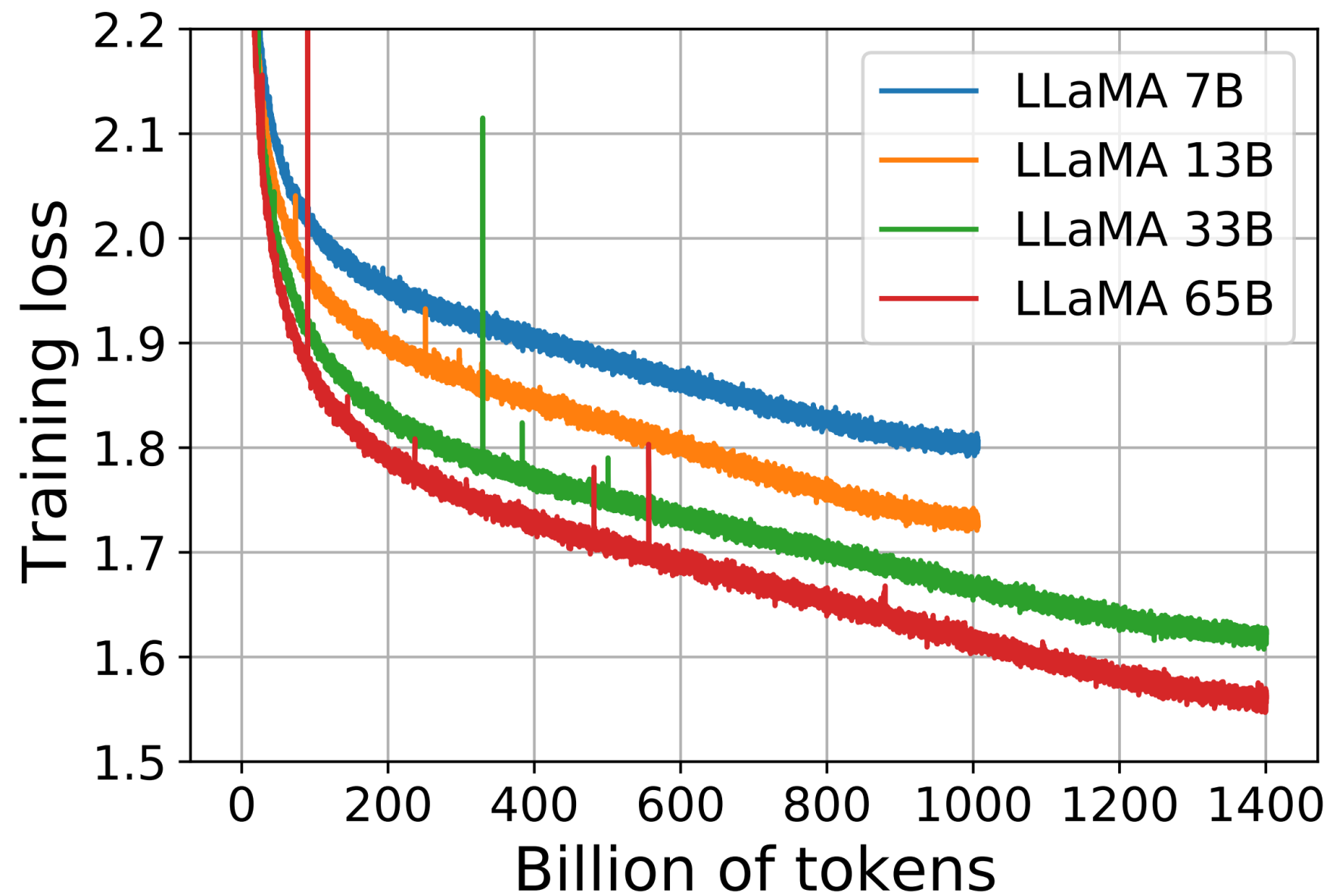
- Web data: large quantities of data
 - Extract, filter, deduplicate to improve quality
 - Filter to cover desired domain(s)
- Mix together web data and other sources to make a pre-training dataset

Recent examples

	Year	Domain	Tokens
FineWeb	2024	Web	15 trillion
RedPajama v2	2024	Web	30 trillion
Dolma	2024	Mix	3 trillion
OLMO2 Mix	2025	Mix	4 trillion
OpenWebMath	2023	Math web pages	15 billion
AlgebraicStack	2023	Math code	11 billion
FineWeb-Edu	2024	Educational (middle-school)	1.4 trillion

Today's lecture

- Tasks
- Data
- **Thinking about pretraining**
 - Tokens, model size, compute
 - Scaling laws



**Bigger
model**



**Better
Loss**



More data

Pretraining and compute

- Goal: get a better pretrained model by “adding more compute”
- *“The biggest lesson that can be read from 70 years of AI research is that general methods that leverage computation are ultimately the most effective, and by a large margin.”*
 - *The Bitter Lesson*, Richard Sutton 2019

What is compute?

- We spend **compute** by performing forward and backward passes on training sequences
- An approximation for transformer language models:

$$C \approx 6ND$$

N : number of model parameters

D : number of tokens

C : compute; floating point operations (FLOPs)

What is compute?

- We spend **compute** by performing forward and backward passes on training sequences
- For example, Llama 2:

$$C \approx 6 \times 7 \text{ billion} \times 2 \text{ trillion}$$

$$= 8.4 \times 10^{22} \text{FLOPs}$$

N : number of model parameters

D : number of tokens

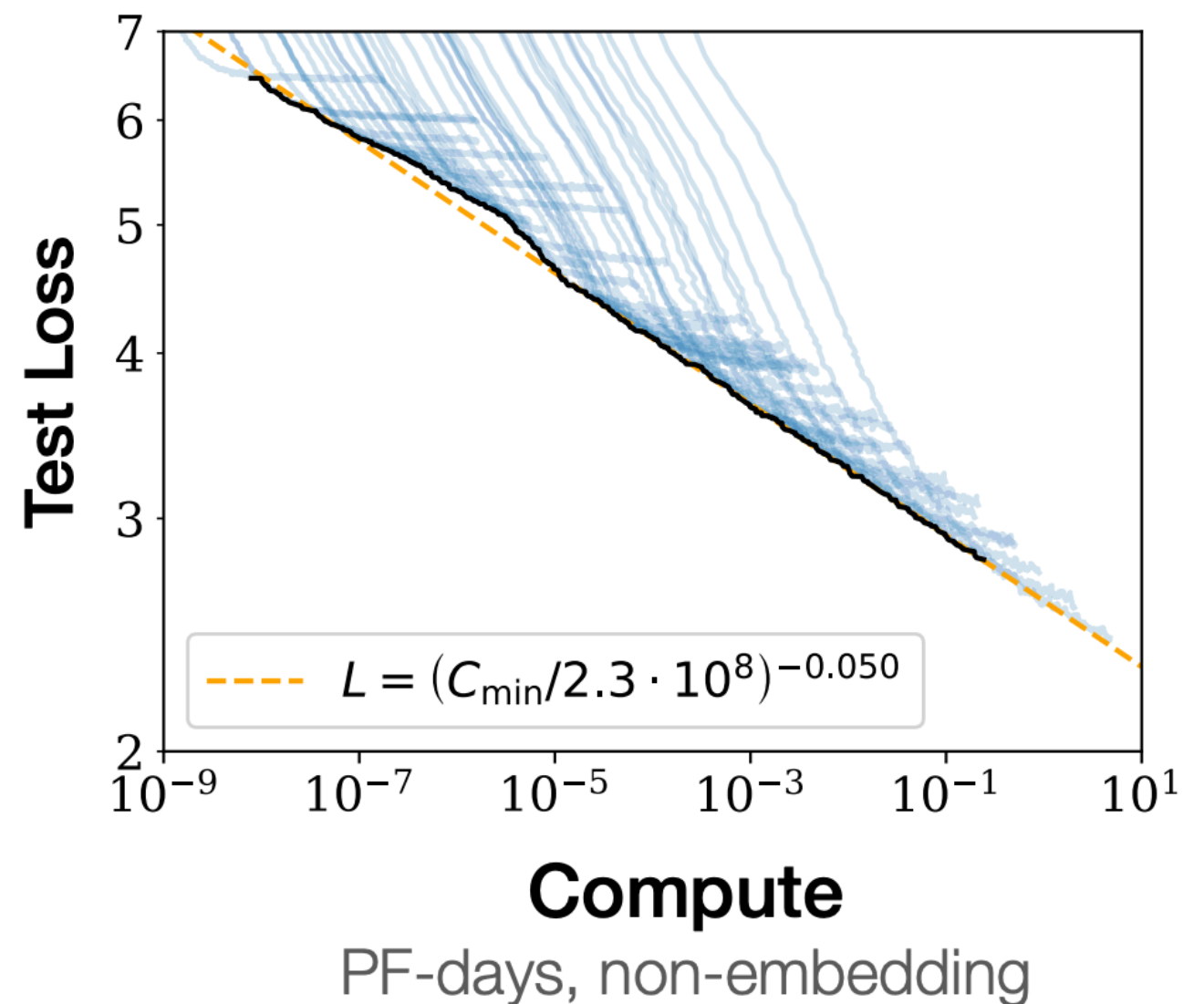
C : compute; floating point operations (FLOPs)

What is compute?

- We spend **compute** by performing forward and backward passes on training sequences
- **Increase compute:**
 - increase the **number of parameters** ($\uparrow N$)
 - train on **more tokens** ($\uparrow D$)

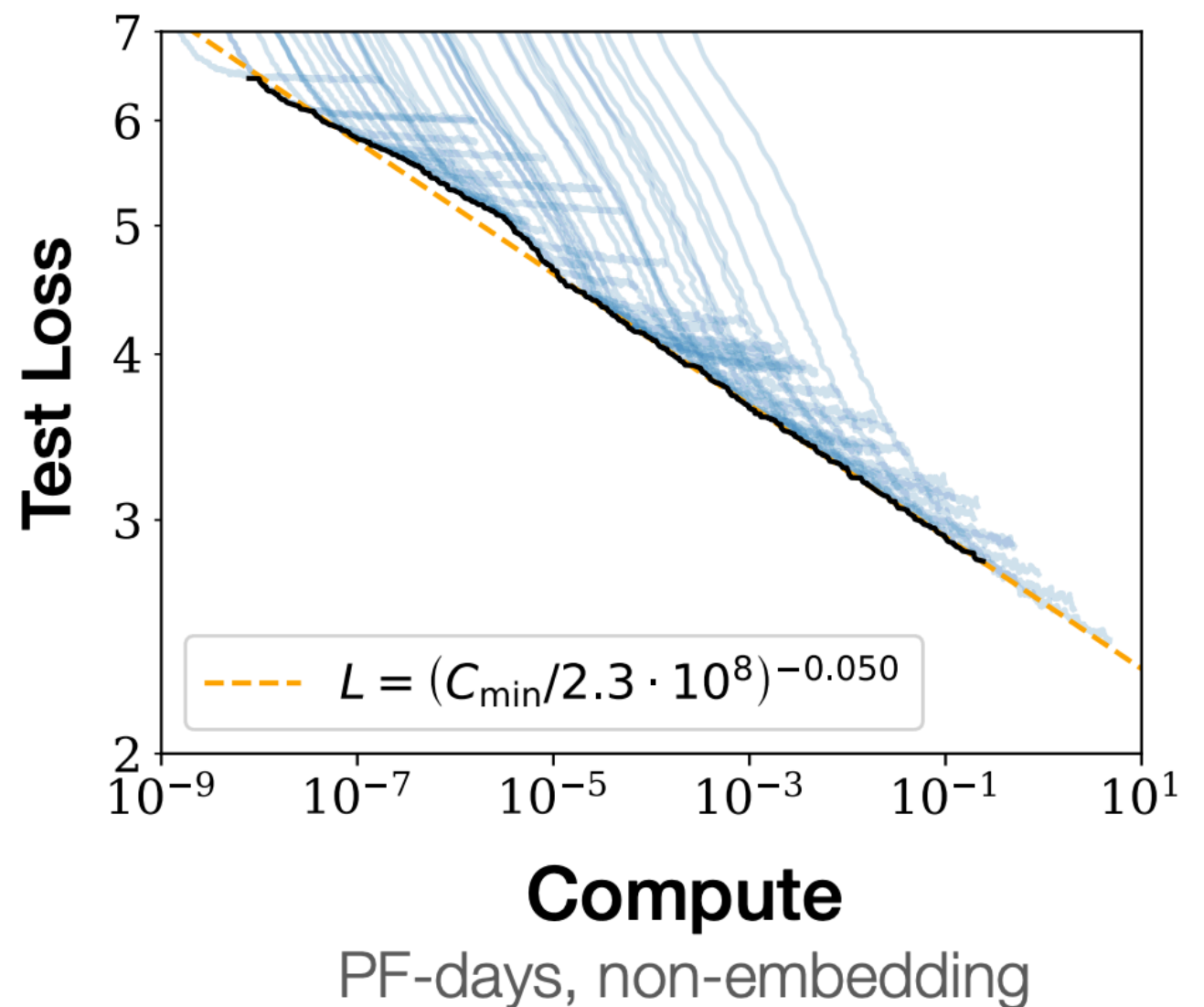
Scaling laws

- Observed relationships between a variable (e.g., amount of compute) and loss



Scaling laws

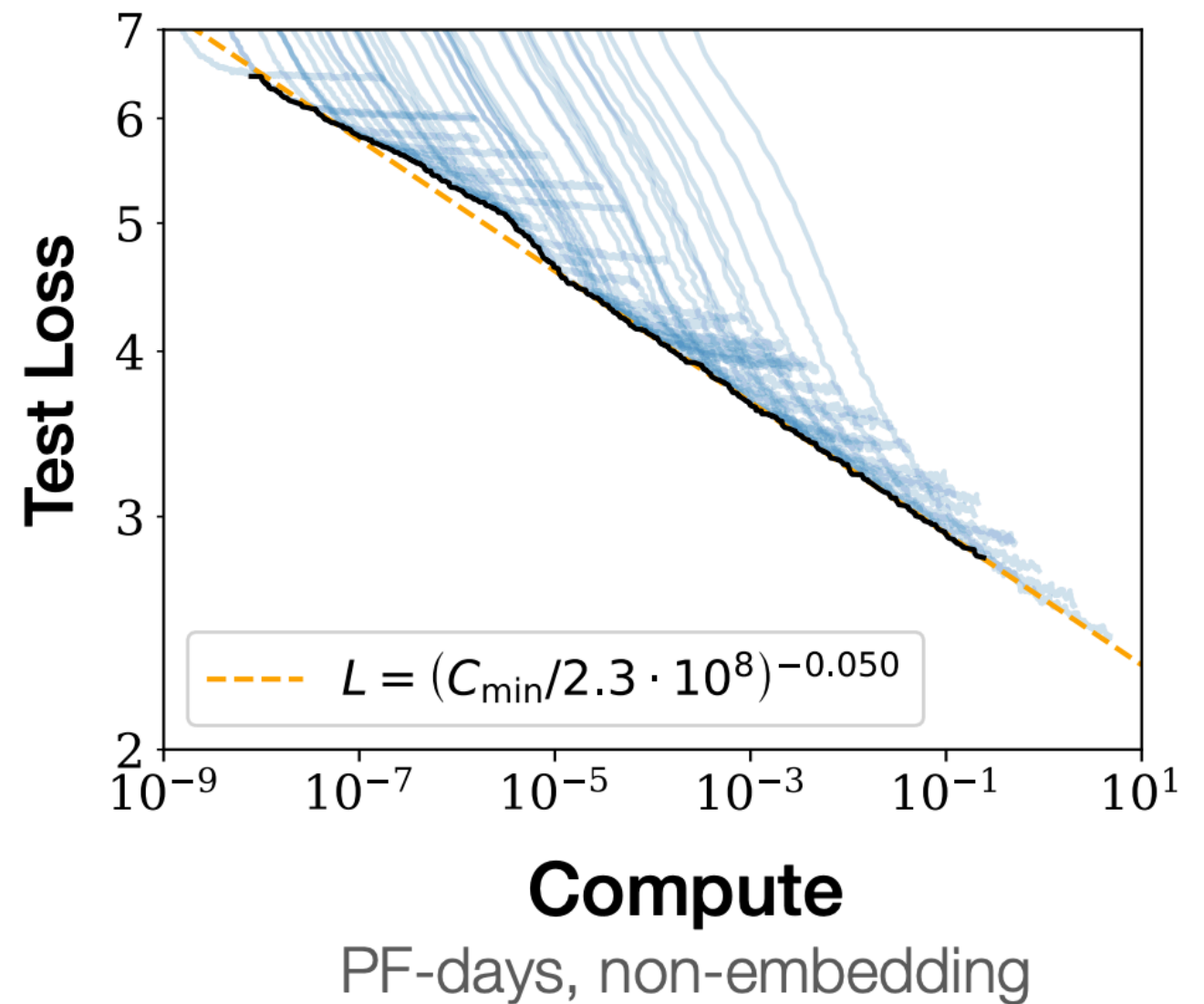
- **Basic idea:**
 - Train models of different sizes and numbers of tokens
 - Plot loss at each step of training [light blue]
 - Pick minimum loss at each amount of compute [black]
 - Run linear regression on the resulting (loss, compute) pairs [orange]



Scaling laws

Terminology:

- **Compute optimal**: black
- **Scaling law**: orange
- E.g. $L(C) \propto 1/C^{0.05}$



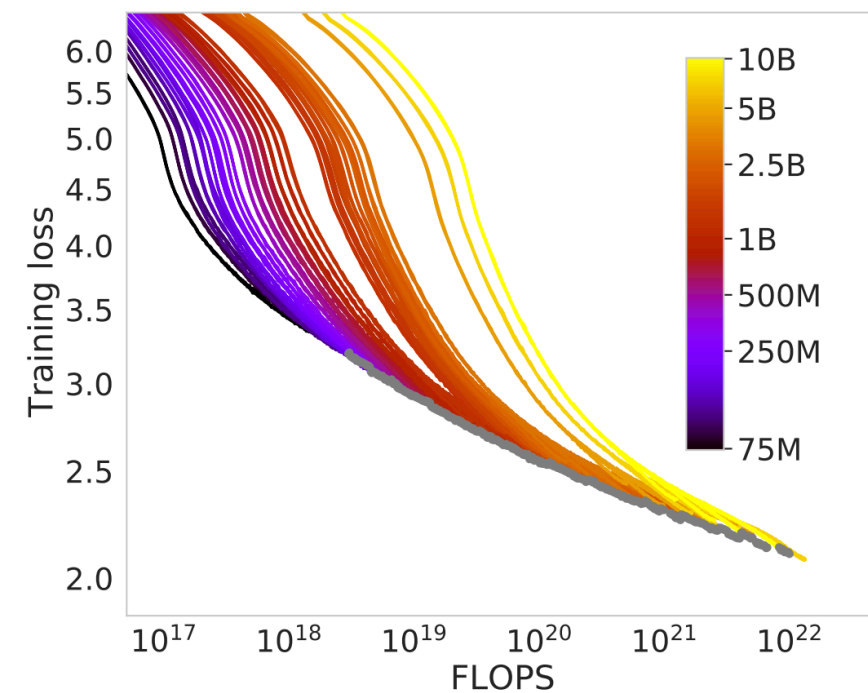
Recap

- We can think of pre-training in terms of *compute*, which is determined by *model size* and *number of tokens*
- *Scaling laws* are observed relationships between a variable (e.g., compute) and loss

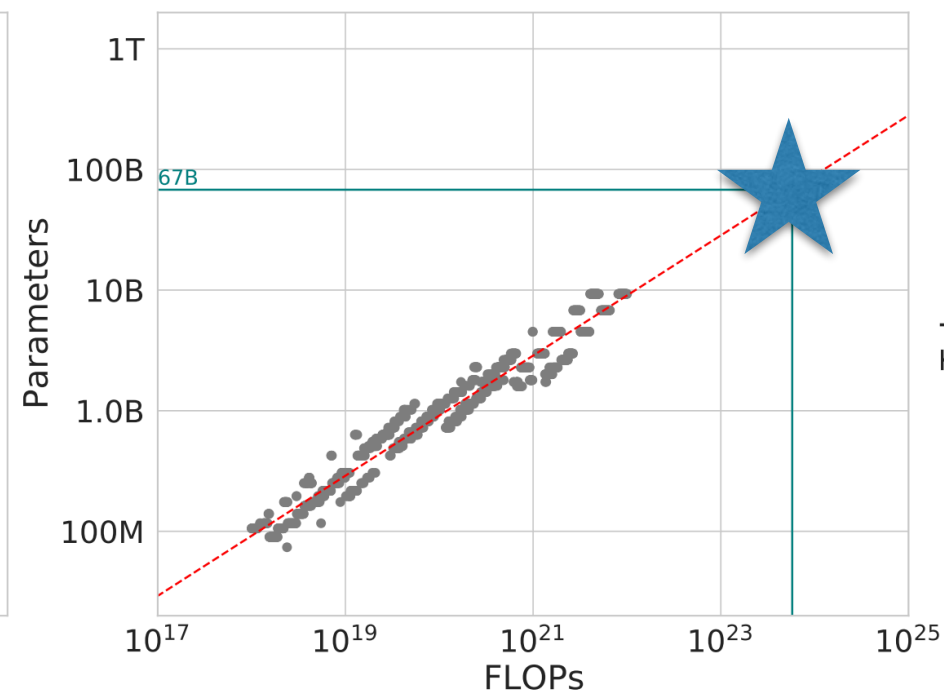
Using scaling laws

- Scaling laws are also used to choose hyper parameters
- Basic idea:
 - Run many experiments at a small scale
 - Use a scaling law to estimate the best hyper parameter for a large-scale model / training run

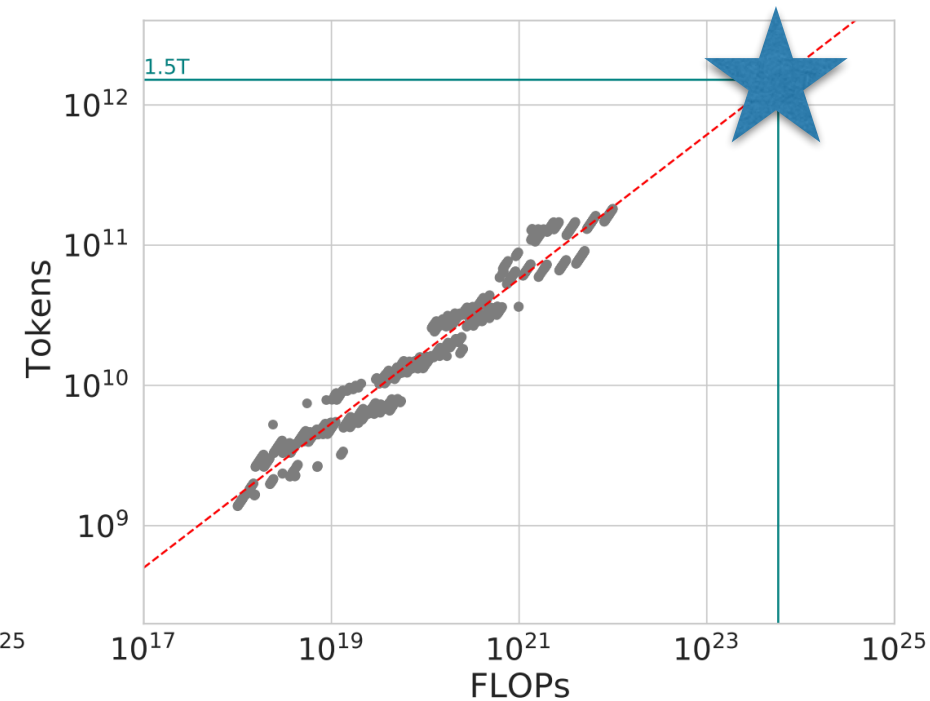
Example: choose model size and # of tokens



Run experiments

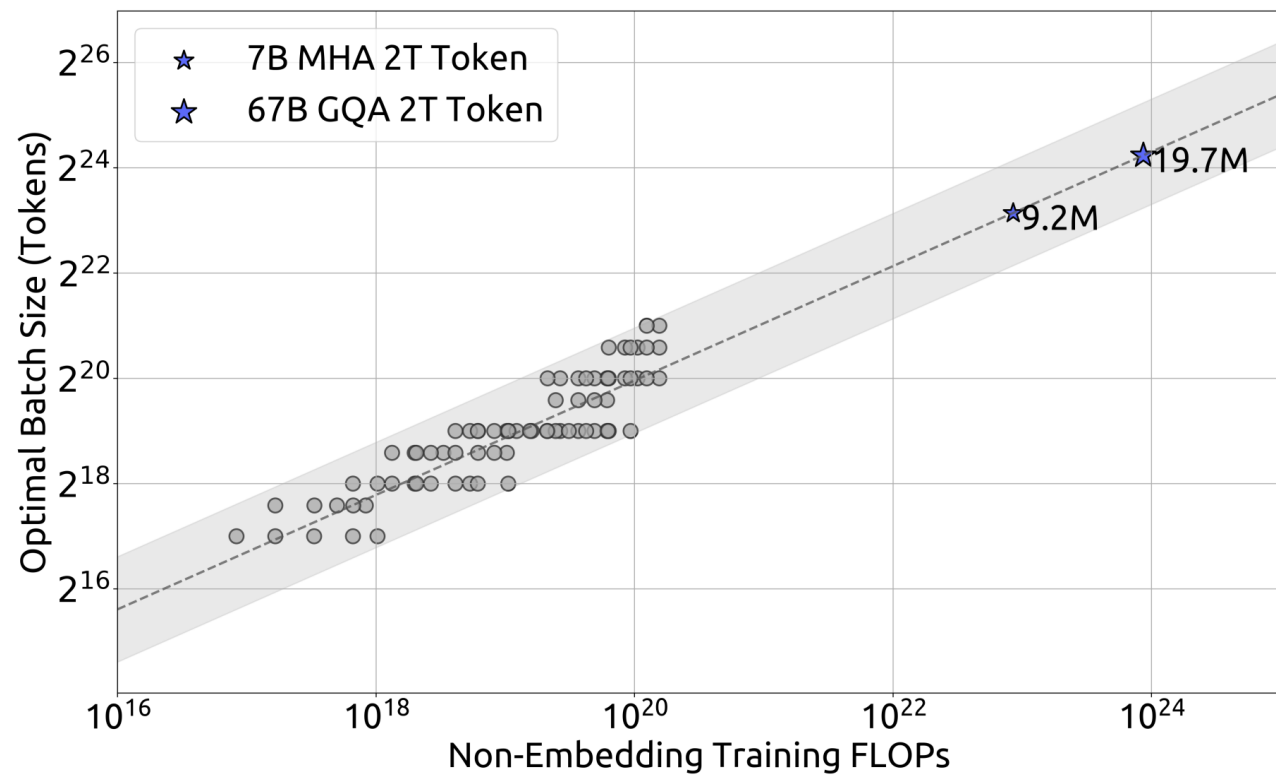


Fit a line and
predict optimal
model size

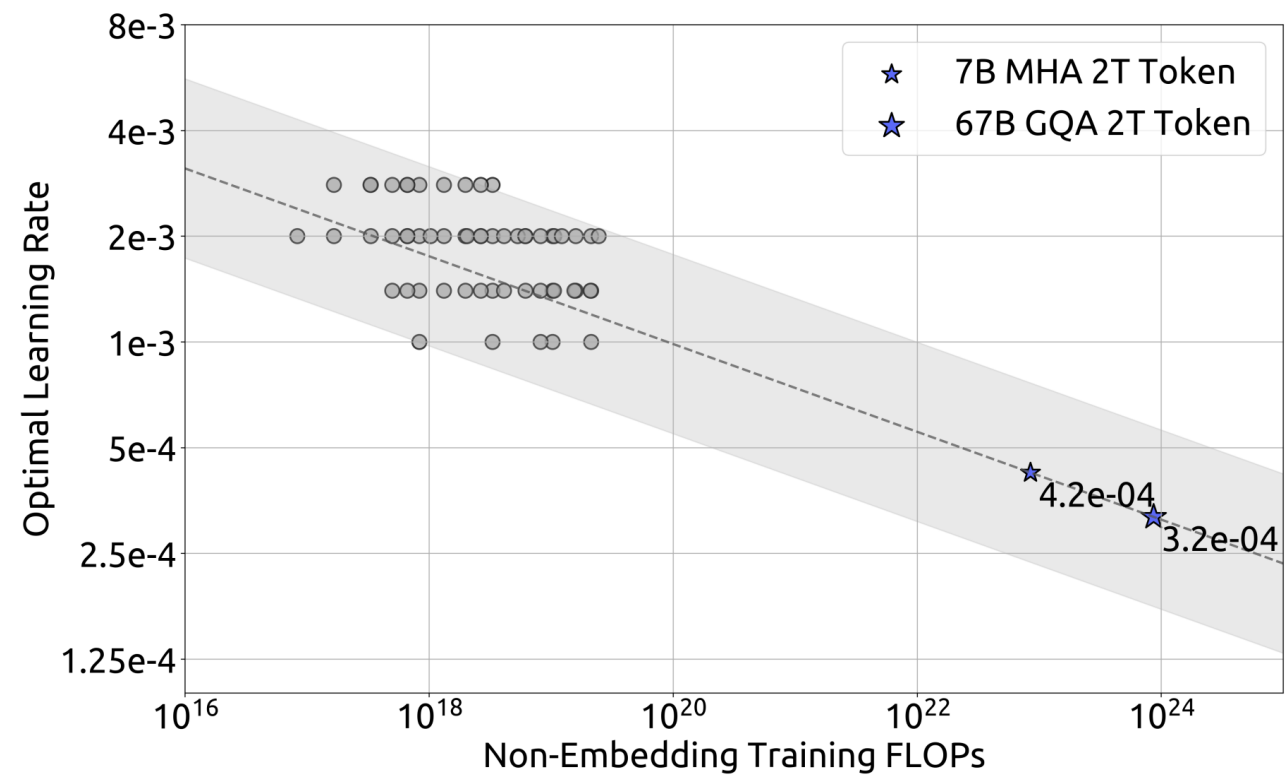


Fit a line and
predict optimal
of tokens

Example: choose batch size, learning rate



Optimal batch size



Optimal learning rate

Today's lecture

- Pretraining tasks
 - Masked language modeling
 - Autoregressive language modeling
- Pretraining data: sources, quality, and quantity
- Thinking about pretraining
 - Tokens, model size, compute
 - Scaling laws

Thank you