

# Beyond Decoding: Meta-Generation Algorithms for Large Language Models

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Presenters: Matthew Finlayson, Hailey Schoelkopf, Sean Welleck

December 11, 2024

Algorithms for generating outputs with a language model

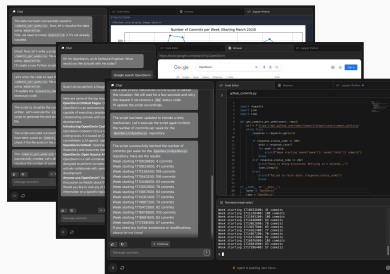
## Algorithms for generating outputs with a language model

Why? Use *test-time compute* to improve performance

# Language models



Solving olympiad problems

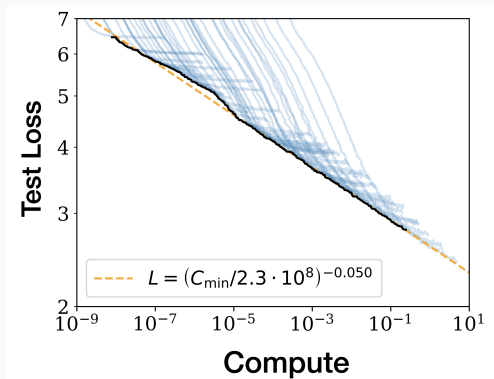


Writing code

Tasks framed as generating sequences: many other applications

# Approach 1: scale pretraining compute

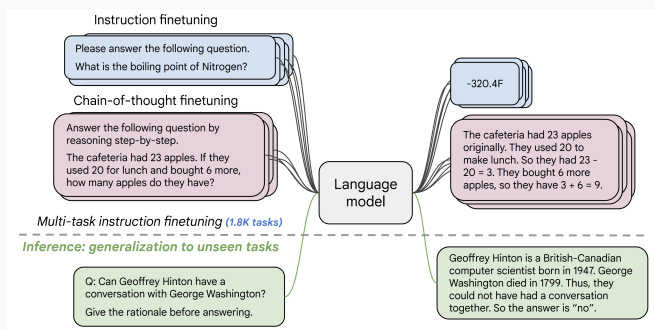
[2020-] Scaling pretraining: larger model, larger dataset



*Scaling Laws for Neural Language Models* [Kaplan et al., 2020]

# Approach 2: scale post-training compute

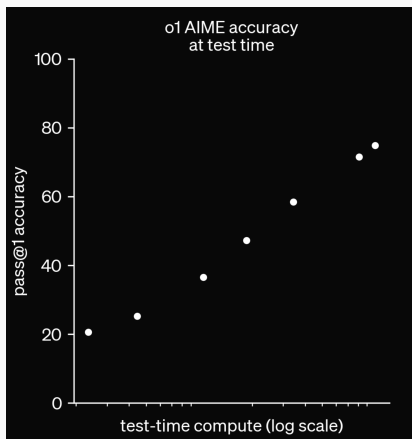
[2022-] Scaling post-training: e.g., fine-tune on (input, output) pairs



Scaling Instruction-Finetuned Language Models [Chung et al., 2022]

## Approach 3: scale *test-time* compute

[Now] Test-time scaling: increase compute at generation time



Test-time compute vs. accuracy ([OpenAI, 2024])

# Approach 3: scale *test-time* compute | How?

## 1. Generate extra tokens

input -> answer

Model Output

A: The answer is 27. ❌

input -> **thought**, answer

Model Output

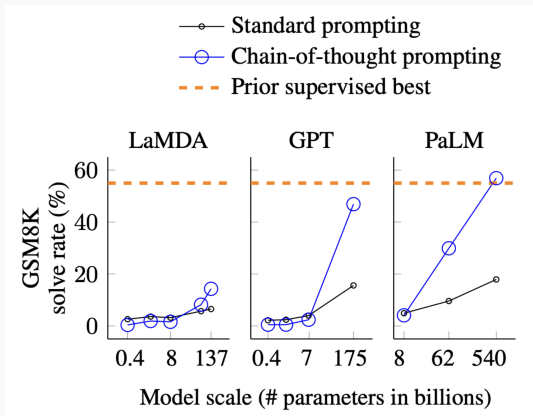
A: The cafeteria had 23 apples originally. They used 20 to make lunch. So they had  $23 - 20 = 3$ . They bought 6 more apples, so they have  $3 + 6 = 9$ . The answer is 9. ✅

[Wei et al., 2022]



# Approach 3: scale *test-time* compute | How?

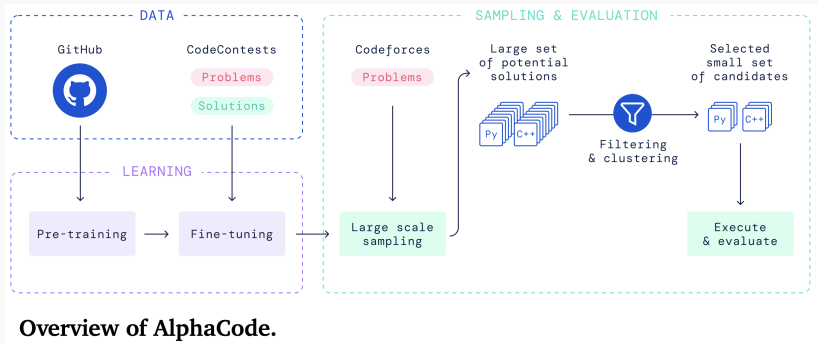
## 1. Generate extra tokens



[Wei et al., 2022]

# Approach 3: scale *test-time* compute | How?

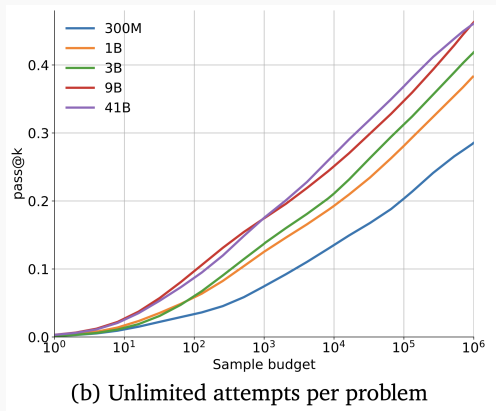
1. Generate extra tokens
2. Call generator multiple times



AlphaCode [Li et al., 2022]

## Approach 3: scale *test-time* compute | How?

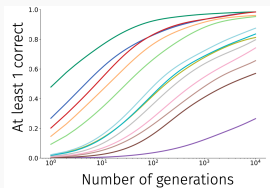
1. Generate extra tokens
2. Call generator multiple times



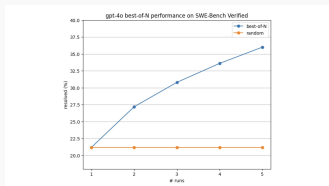
AlphaCode [Li et al., 2022]

# Approach 3: scale *test-time* compute | How?

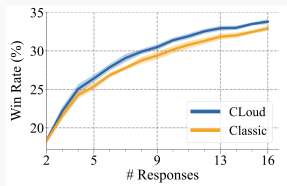
1. Generate extra tokens
2. Call generator multiple times



Math [Brown et al., 2024]



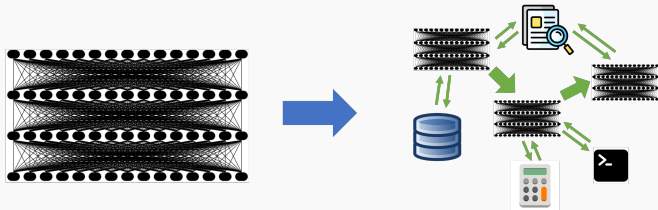
Agents [Nebius, 2024]



Chat [Ankner et al., 2024]

## Approach 3: scale *test-time* compute | How?

1. Generate extra tokens
2. Call generator multiple times
3. Incorporate other models/tools



[Zaharia et al., 2024]

Verifiers, code interpreters, search engines, ...

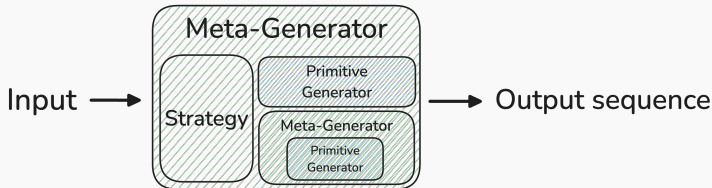
**This tutorial:** *How? Meta-Generation Algorithms*

**Generator:** Generates a sequence with a language model.



- Example: calling an LLM API
- Traditional algorithms
  - Greedy decoding
  - Temperature sampling
  - ...

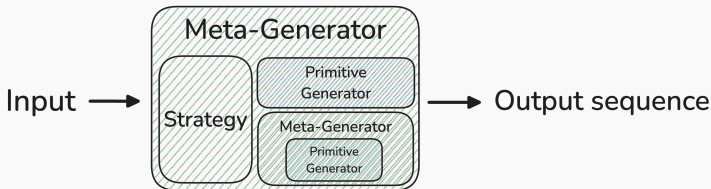
**Meta-generator:** High-level strategies for calling generators and using external information.



- Example: call API multiple times, select the best sequence with a separate model



**Meta-generator:** High-level strategies for calling generators and using external information.



Why?

- Generate more to improve task performance
- Combine multiple models (verifiers, retrievers, ...)
- Incorporate external information (tools, feedback, ...)

## *Beyond Decoding: Meta-Generation Algorithms for LLMs*

- I: **Primitive generators:** Generating one token at a time
- II: **Meta-generators:** High-level strategies for calling generators
- III: **Efficient meta-generation:** Generating quickly and efficiently

Panel session at the end!

# Presenters

## Part I



Matthew Finlayson

USC

@mattf1n

## Intro/Part II



Sean Welleck

CMU

@wellecks

## Part III



Hailey Schoelkopf

EleutherAI

@haileysch\_\_

# Panel



**Beidi Chen**

CMU

@BeidiChen



**Nouha Dziri**

AI2

@nouhadziri



**Rishabh Agarwal**

DeepMind/McGill

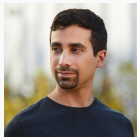
@agarwl\_



**Jakob Foerster**

Oxford/Meta AI

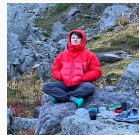
@j\_foerst



**Noam Brown**

OpenAI

@polynoamial



**Ilia Kulikov (Moderator)**

Meta AI

@uralik1

## Neurips 2024 Tutorial: Beyond Decoding: Meta-Generation Algorithms for Large Language Models



Sean Welleck<sup>1</sup>



Amanda Bertsch<sup>1</sup>



Matthew Finlayson<sup>2</sup>



Alex Xie<sup>1</sup>



Graham Neubig<sup>1</sup>



Konstantin Golobokov<sup>5</sup>



Hailey Schoelkopf<sup>3</sup>



Iliia Kulikov<sup>4</sup>



Zaid Harchaoui<sup>5</sup>

<sup>1</sup>Carnegie Mellon University

<sup>2</sup>University of Southern California

<sup>3</sup>Work done while at EleutherAI




<sup>4</sup>Meta AI

<sup>5</sup>University of Washington




Survey (TMLR 2024): *From Decoding to Meta-Generation:  
Inference-time Algorithms for Large Language Models* [Welleck et al., 2024]

[cmu-l3.github.io/neurips2024-inference-tutorial](https://cmu-l3.github.io/neurips2024-inference-tutorial)

Code examples, reading list, slides

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